

**2-1 The Language of Functions**

**Goal:** Give definitions, properties and representations of functions

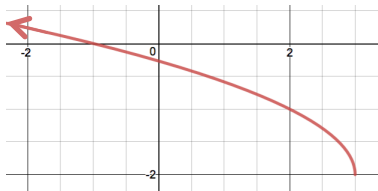


Questions

**Notes**

**Warm Up:** Determine whether the relation is a function in 1-2. Explain. Then list the domain and range.

1.



2.

$x$	$y$
1	-2
-1	2
-2	4
1	3

**Vocabulary**

relation:

independent variable:

dependent variable:

**What is a Function?**

A **function** is a \_\_\_\_\_  $(x, y)$  in which each first component  $(x)$  is paired with \_\_\_\_\_ second component  $(y)$ .

Example  
 $f = \{(1,2), (2,4), (3,7)\}$

Non-example  
 $g = \{(1,2), (2,4), (1,7)\}$

**domain:**

**range:**

## Questions

real functions:

The symbol	represents the set of all
$\mathbb{Z}$	integers.
$\mathbb{R}$	real numbers.
$\mathbb{Q}$	rational numbers.
$\mathbb{N}$	natural numbers.

**Example 1:** A bakery charges \$2.00 per muffin. Customers get a \$2.00 discount for every 6 muffins purchased.

- Which statement is true: “the cost  $c$  is a function of the number  $m$  of muffins” or “the number  $m$  of muffins is a function of the cost  $c$ ?”
- Identify the independent and dependent variables of the function.
- State the domain and range of the function.

**Example 2:**

The Sudoku Club at a high school needs t-shirts for their upcoming tournament. They were able to negotiate a “buy-two-get-one-free” deal from a local store. The cost for one t-shirt is \$10.

- Which statement is true: “the cost  $c$  is a function of the number  $t$  of t-shirts” or “the number of t-shirts  $t$  is a function of the cost  $c$ ?”
- Identify the independent and dependent variables of the function.
- State the domain and range of the function.

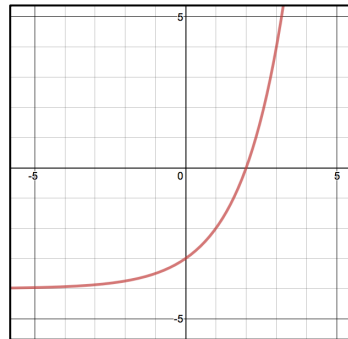
**Descriptions of Functions**

Three ways to describe/represent functions are:

- 1.
- 2.
- 3.

**Example 3:** A rule for the function graphed at the right is  $y = 2^x - 4$ .

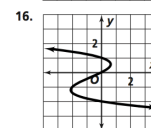
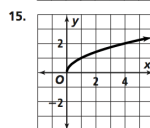
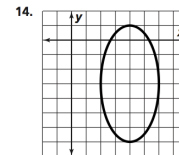
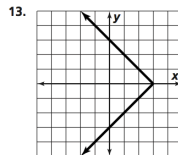
Find the domain and range of the function.



**Example 4:** Find the domain and range of the function with the rule

$$y = 3(x - 5)^2 - 1.$$

**Testing for Functions:** Use the *vertical line test* to determine which are functions to the right.

**Questions**

**Questions****Naming Functions & Their Values**

Functions can be named with letters, such as  $f$  or  $g$ . The symbol  $f(x)$  is read “\_\_\_\_\_”.

**Example 5:** Suppose  $f$  is defined by the rule  $f(x) = 4 \cdot \left(\frac{1}{2}\right)^x$  for all real numbers  $x$ .

a. Evaluate  $f(5)$

b. Does  $f(-2+3) = f(-2) + f(3)$ ?

c. Evaluate  $f(n+1)$ .

**Example 6:** Suppose  $g$  is defined by the rule  $g(x) = 2x^2 - 3x - 2$  for all real numbers  $x$ .

a. Evaluate  $g(-2)$

b. Does  $g(-2+3) = g(-2) + g(3)$ ?

c. Evaluate  $g(2n-1)$ .